

Quantum Mechanics: from fundamental problems to applications
2006

Bertinoro

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Degenerate quantum gases in periodic and disordered potentials

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<http://quantumgases.lens.unifi.it>

Bose–Einstein condensates in periodic and disordered potentials

- Superfluid to Mott insulator transition
- Disordered potentials

Quantum degenerate mixtures

- Ultracold heteronuclear molecules
- Attractive condensates for Quantum Measurements

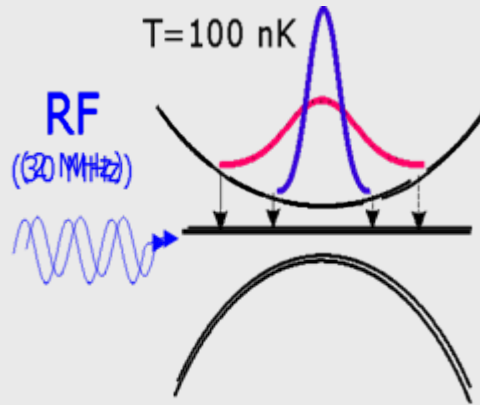
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Bose–Einstein condensation of alkali atoms



“Magneto–optical trap”, i.e. laser + weak magnetic quadrupole:

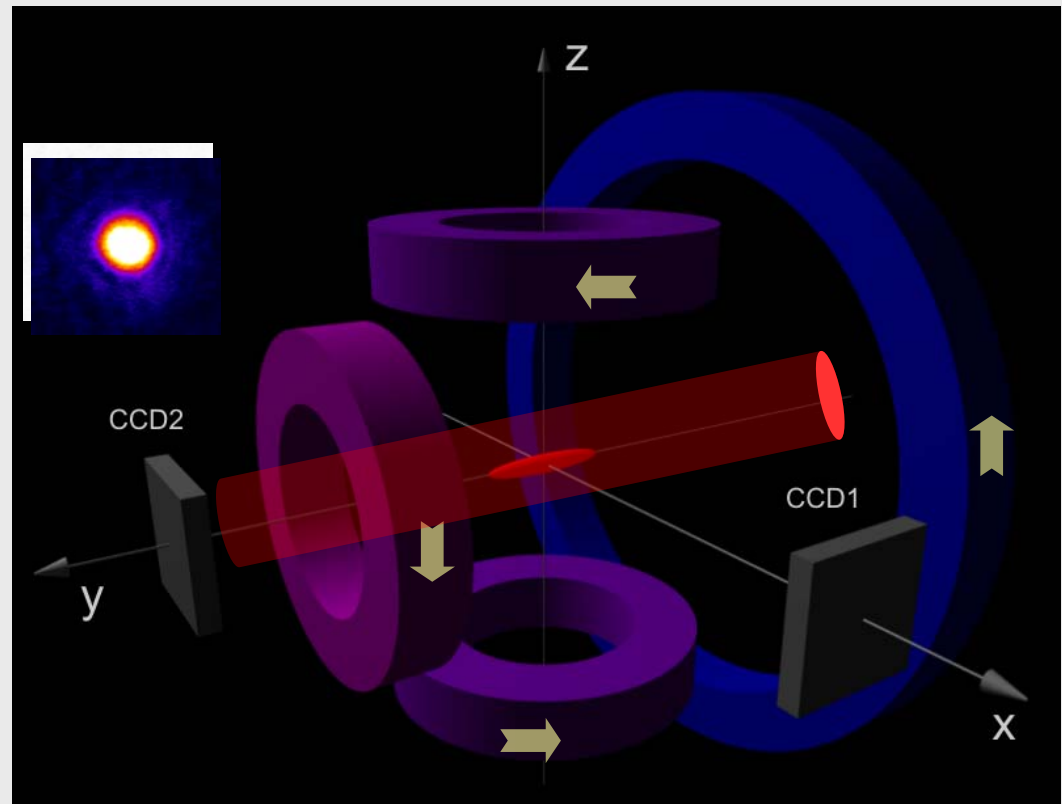
Natoms $\sim 10^9$, Temperature $\sim 100 \mu\text{K}$, $\log(\text{PSD}) \rightarrow -7$

Purely magnetic trap, i.e. high magnetic fields confine the atoms in harmonic potential

Forced evaporative cooling to BEC:

Natoms $\sim 10^5$, Temperature $\sim 100 \text{ nK}$

Destructive detection:
release the atoms from trap followed by
absorption imaging, i.e. CCD detection of
the shadow cast on resonant light beams

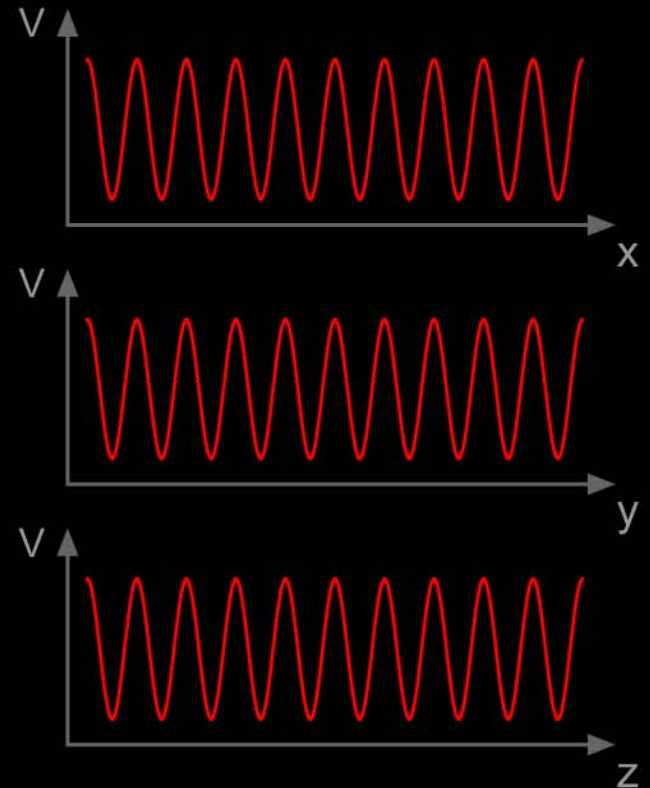
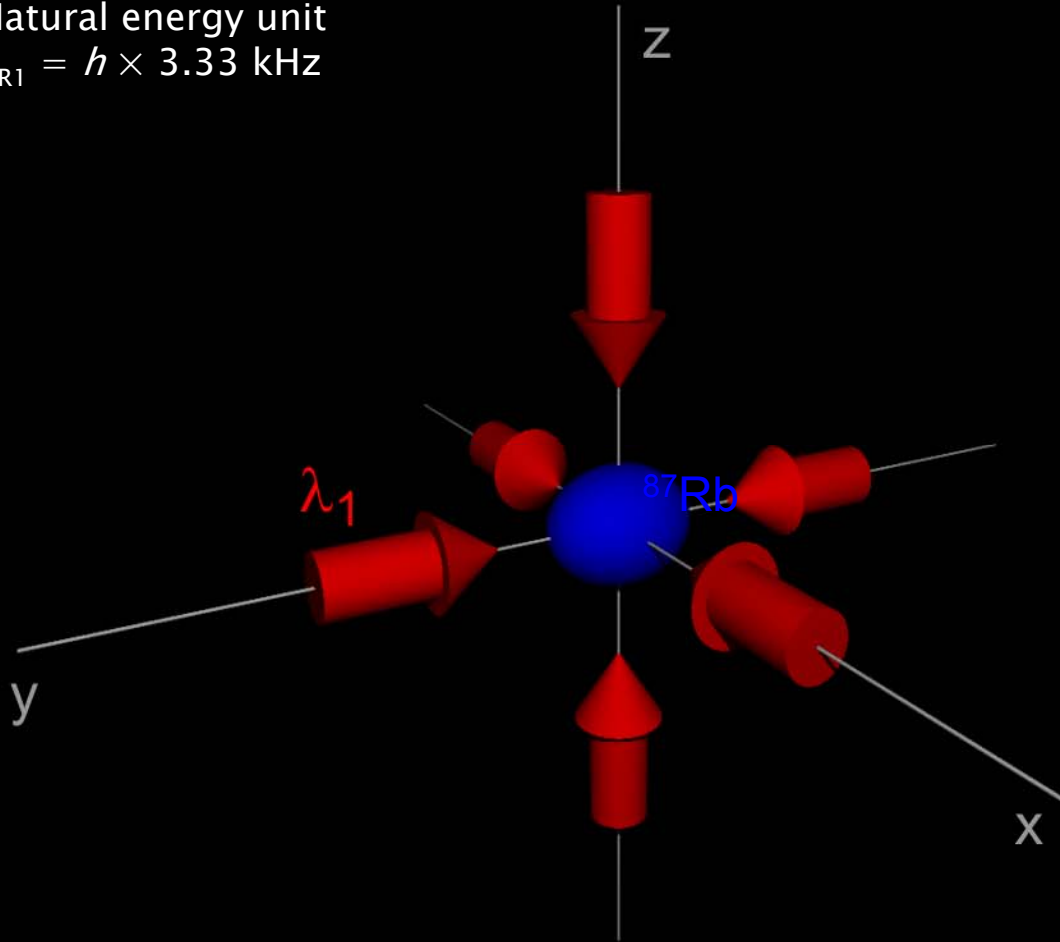


Optical potentials

3 counterpropagating beams, far off-resonant:
conservative potential proportional to intensity, standing wave \rightarrow perfect sine potential

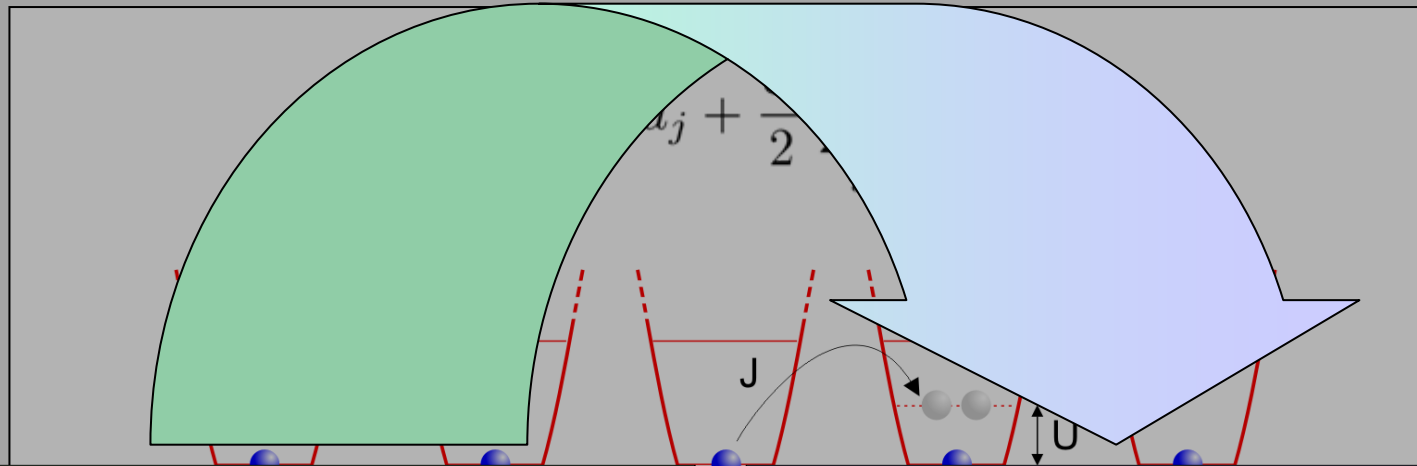
Natural energy unit

$$E_{R1} = h \times 3.33 \text{ kHz}$$



Interacting bosons in a lattice

Bose-Hubbard model for interacting bosons in a lattice:



SUPERFLUID

$$J \gg U$$

- ✓ Long-range phase coherence
- ✓ High number fluctuations
- ✓ Gapless excitation spectrum

MOTT INSULATOR

$$J \ll U$$

- ✓ No phase coherence
- ✓ Zero number fluctuations (Fock states)
- ✓ Gap in the excitation spectrum

hopping energy

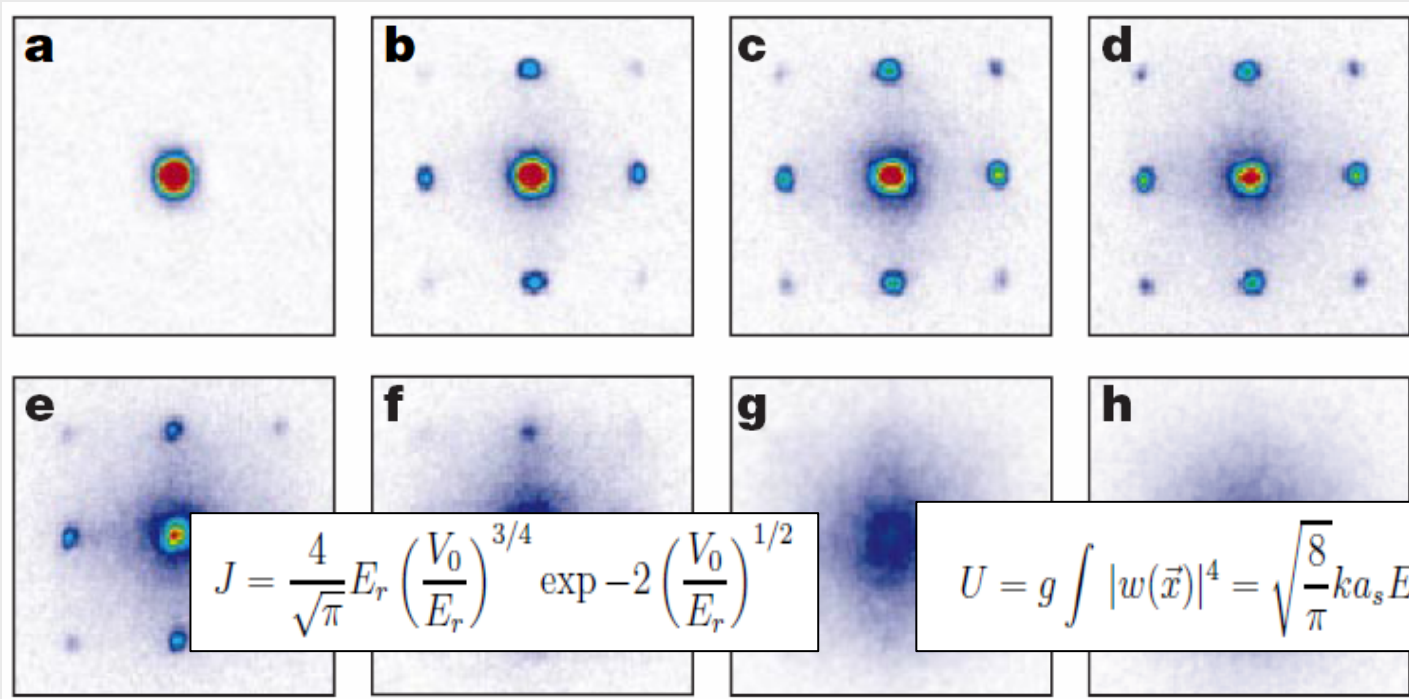
J

interaction energy

U

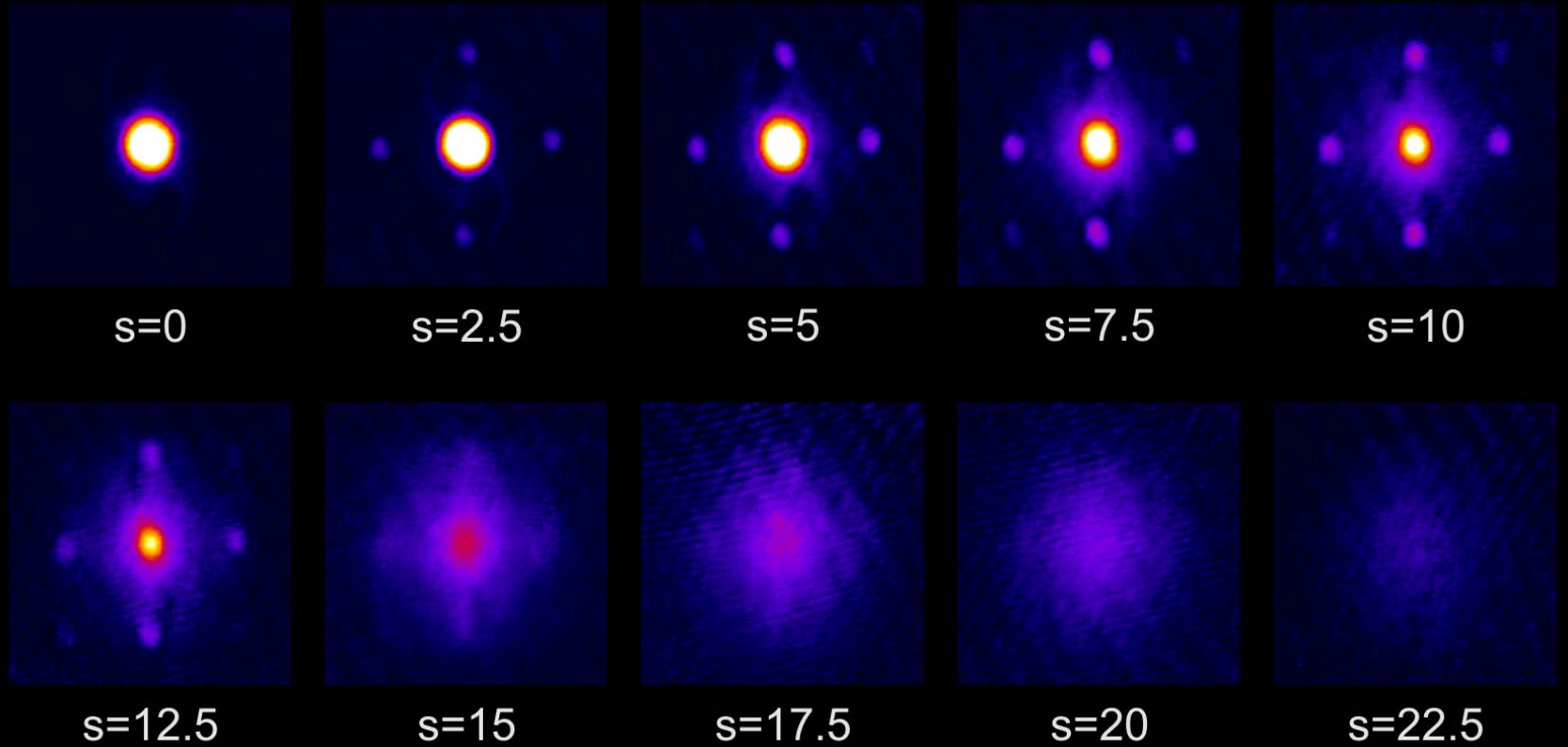
Quantum phase transition from a superfluid to a Mott insulator in a gas of ultracold atoms

Markus Greiner^{*}, Olaf Mandel^{*}, Tilman Esslinger[†], Theodor W. Hänsch^{*} & Immanuel Bloch^{*}



Vanishing interference pattern \longrightarrow loss of long range coherence, phase fluctuations

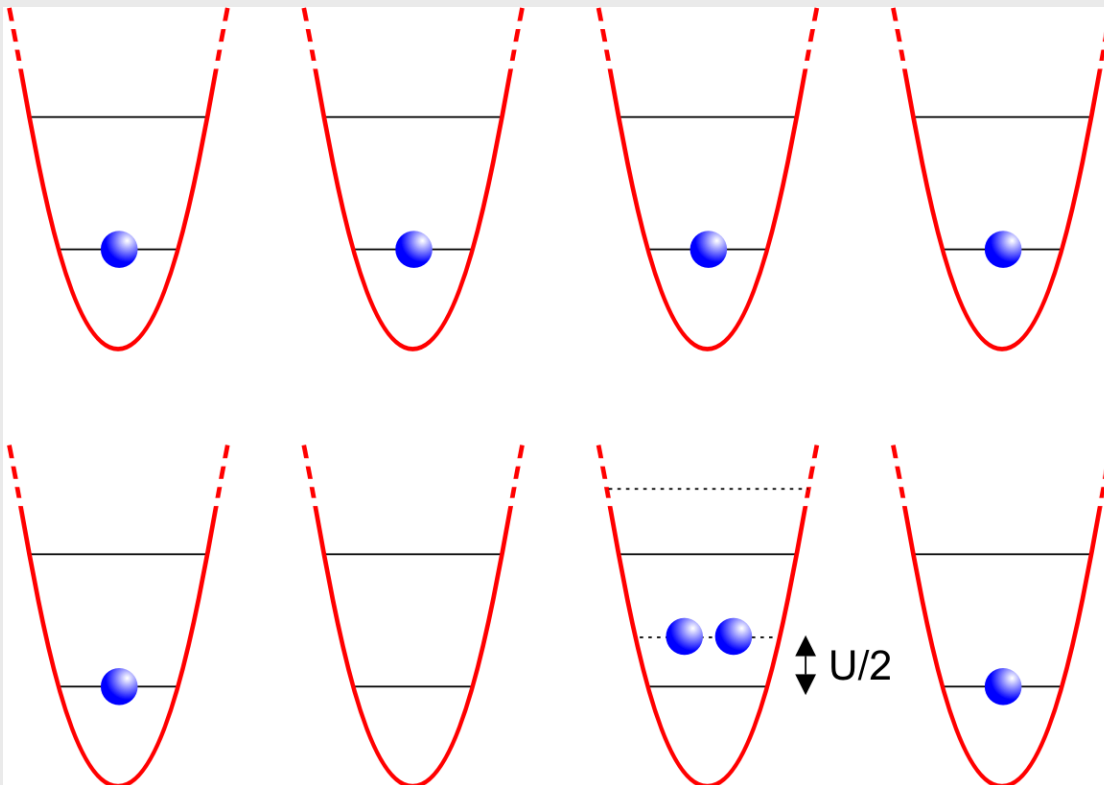
Increasing the lattice height V_0 \longrightarrow J decreases \longrightarrow U increases \longrightarrow U/J increases



Excitation of a Mott Insulator

The elementary excitation of a Mott Insulator consists in the tunnelling of one atom from a lattice site to a neighboring one, thereby increasing the total energy of the system:

$$\hat{H} = -J \sum_{\langle i,j \rangle} \hat{a}_i^\dagger \hat{a}_j + \sum_i \frac{U}{2} (\hat{n}_i - 1) \hat{n}_i$$

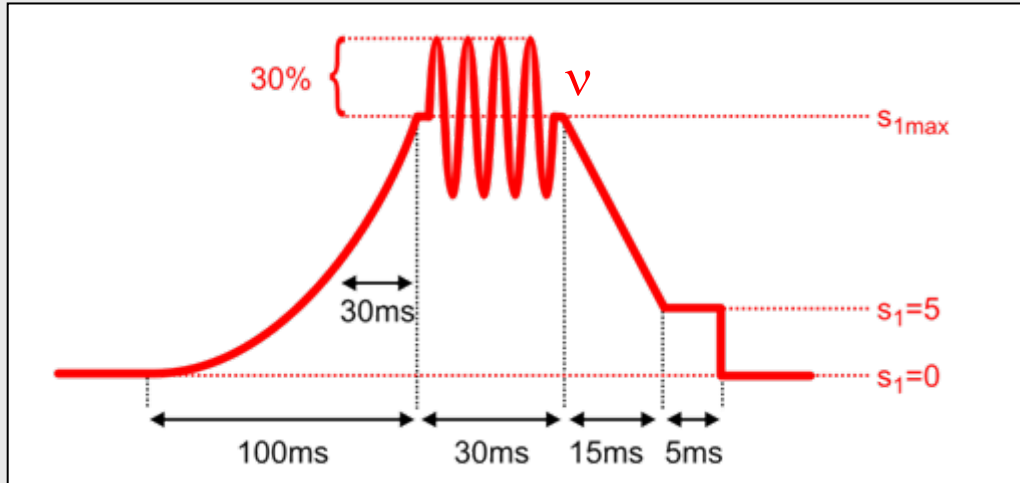


$$E = E_0$$

$$E = E_0 + U$$

Measuring the excitation spectrum

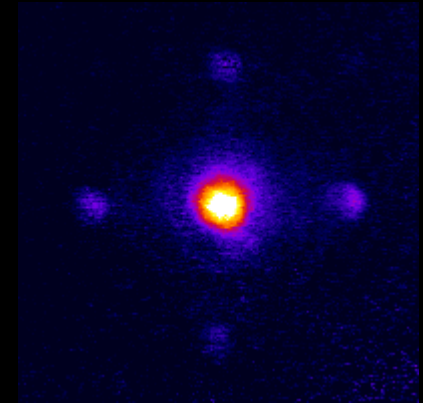
Excitation of the system with an amplitude modulation of the lattice potential along y at frequency ν :



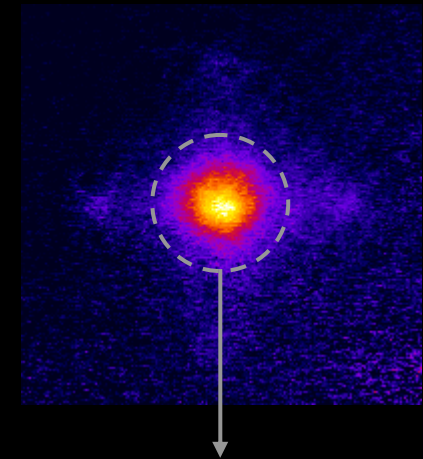
Resonant production of (particle-hole) excitations along y direction at energy $\hbar\nu$

experimental technique introduced in
T. Stöferle et al., *PRL* 92, 130403 (2004)

without modulation:

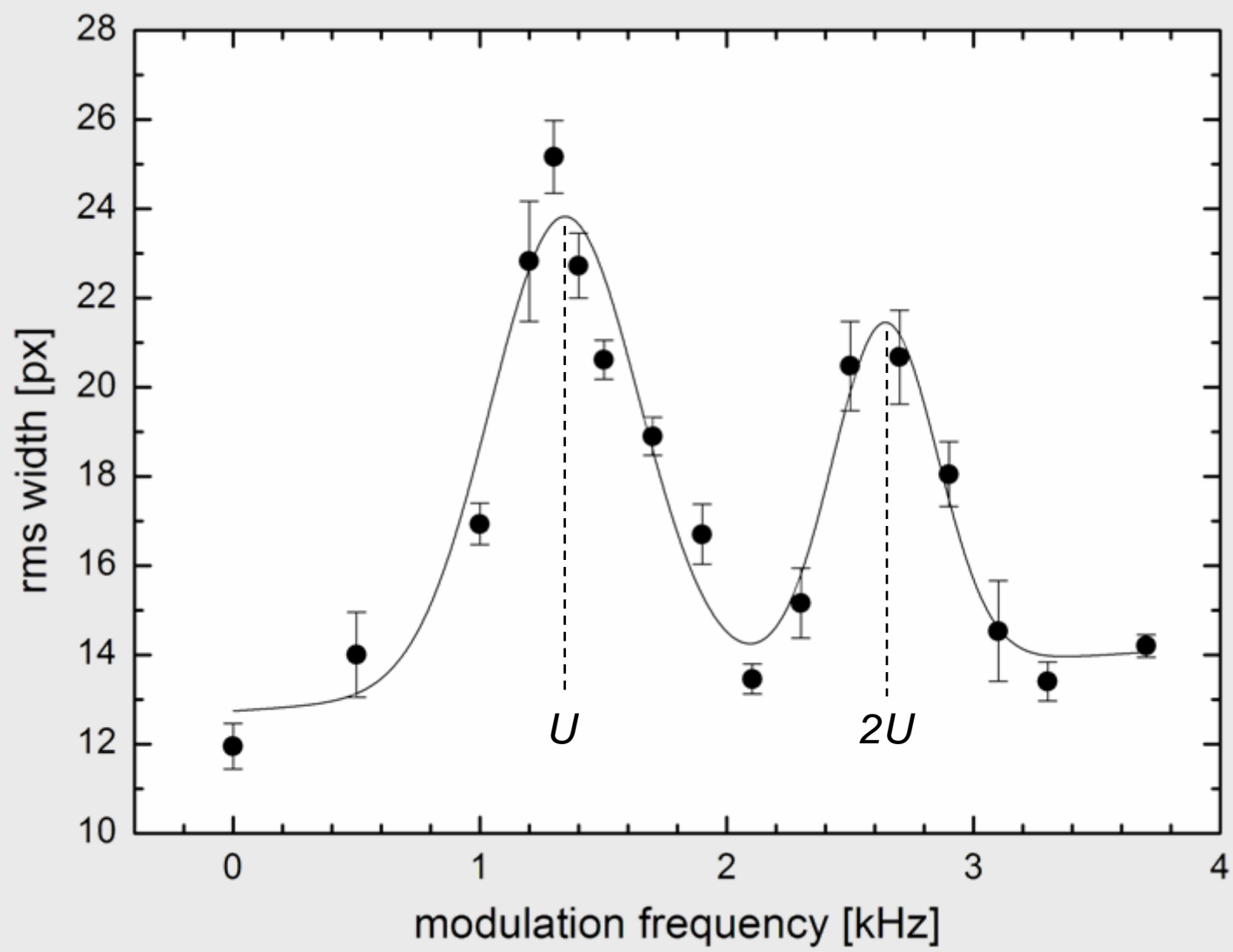


with modulation:



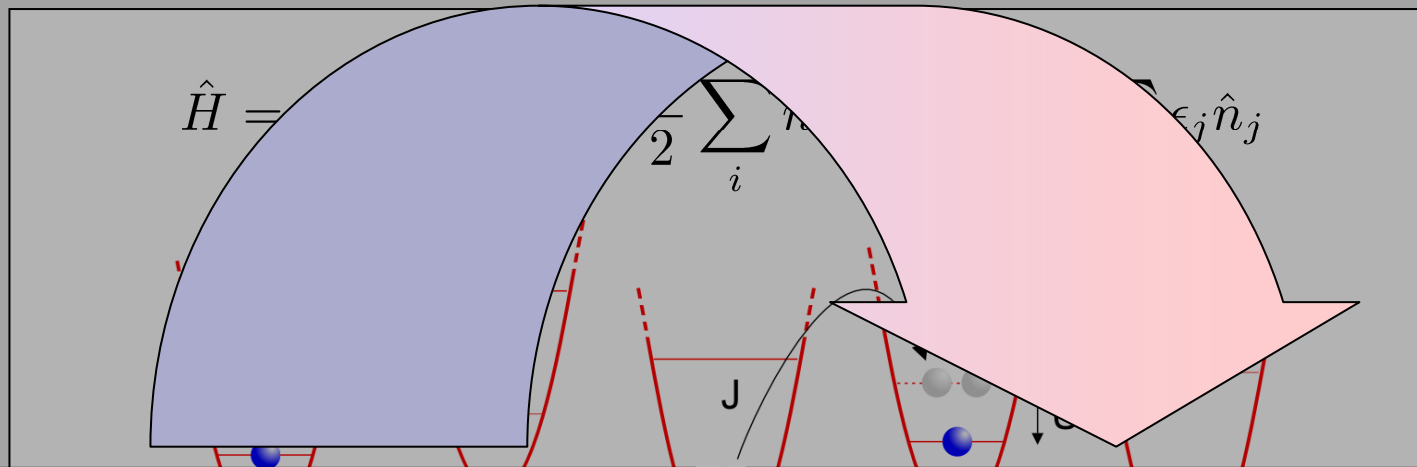
measurement of the width of the central density peak
(energy transfer)

Excitation spectrum of the Mott Insulator



Adding disorder

Bose-Hubbard model with bounded disorder in the external potential $\epsilon_j \in [-\Delta/2, \Delta/2]$



MOTT INSULATOR

$$\Delta \ll U$$

- ✓ No long-range phase coherence
- ✓ Zero number fluctuations
- ✓ Gap in the excitation spectrum

BOSE-GLASS

$$\Delta > U$$

- ✓ No long-range phase coherence
- ✓ Small number fluctuations
- ✓ Gapless excitation spectrum

hopping energy

J

interaction energy

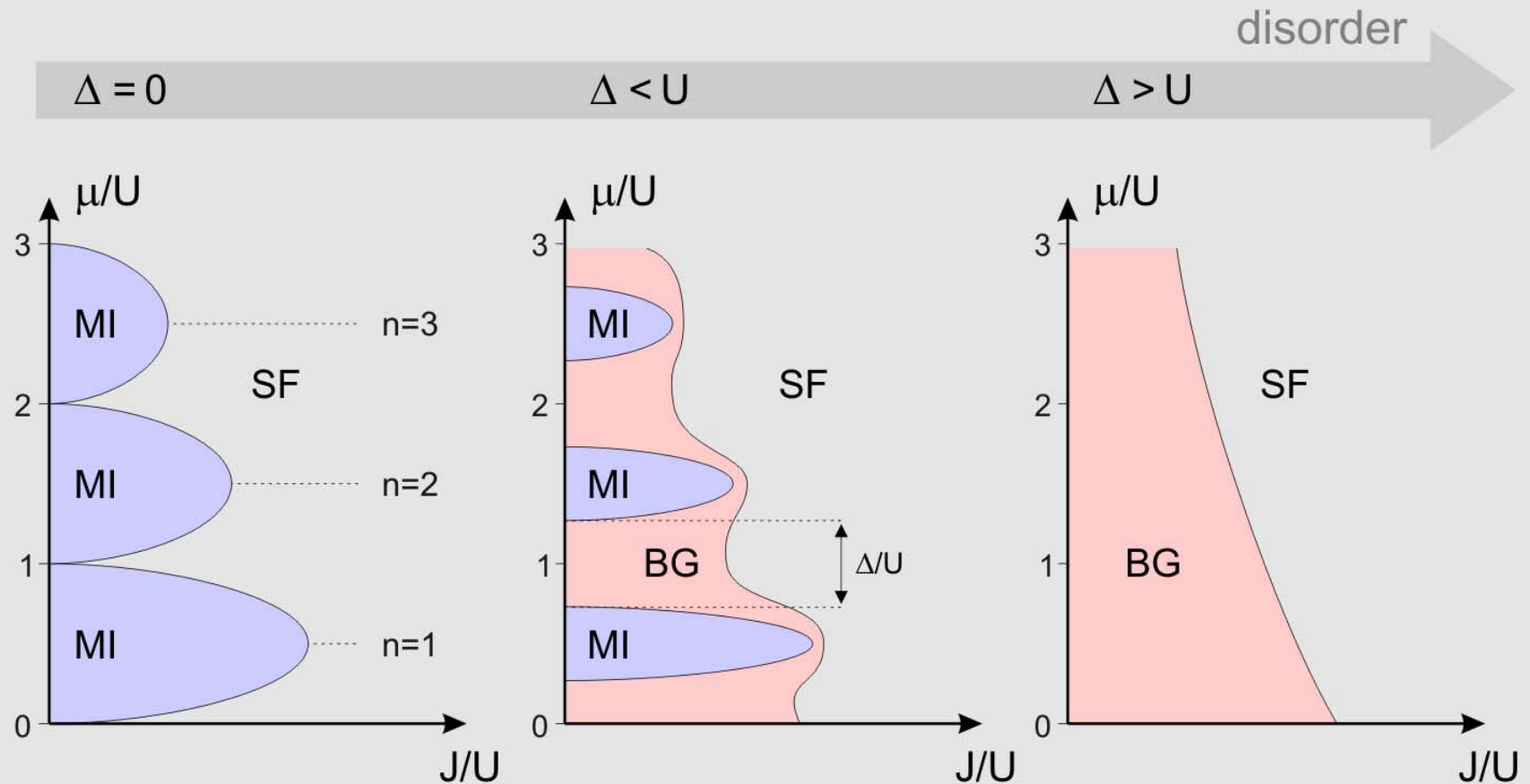
U

disorder

Δ

Phase diagrams

Qualitative phase-diagram for an interacting bosons in a disordered lattice:

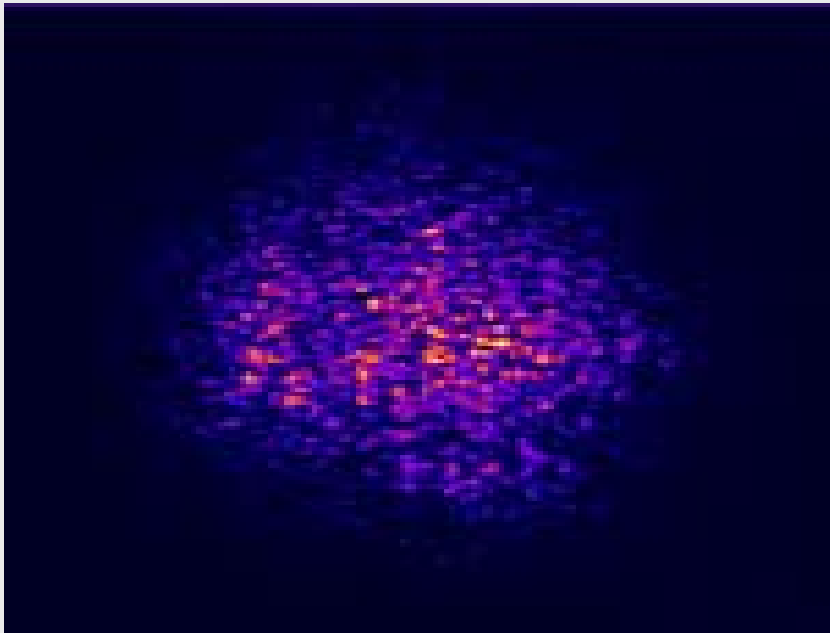


see M. P. A. Fisher et al., *PRB* **40** 546 (1989).

Adding disorder in a controlled manner

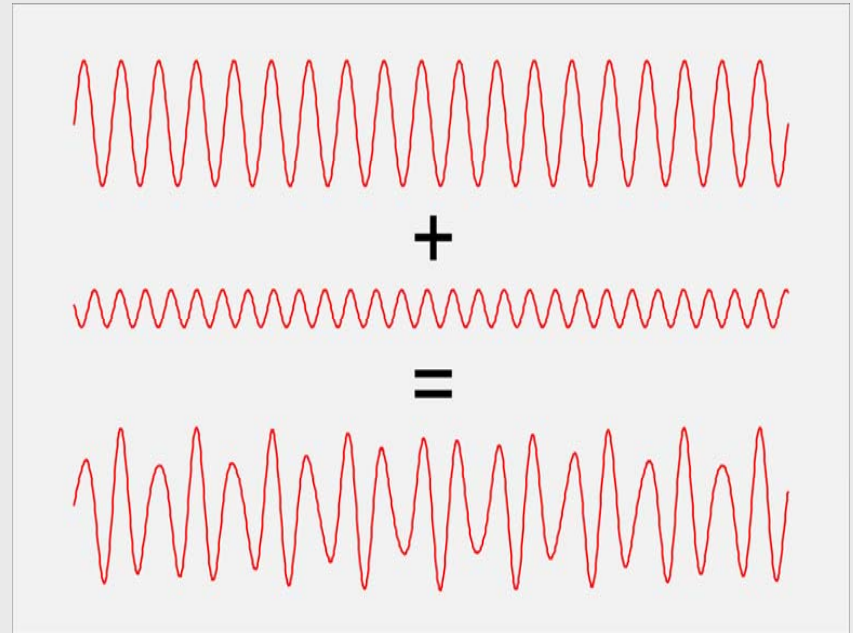
For ultracold atoms in optical lattices one can add optical disorder in two ways:

speckle pattern



- ✓ random potential
- ✗ large length scale (several mm)

bichromatic lattice

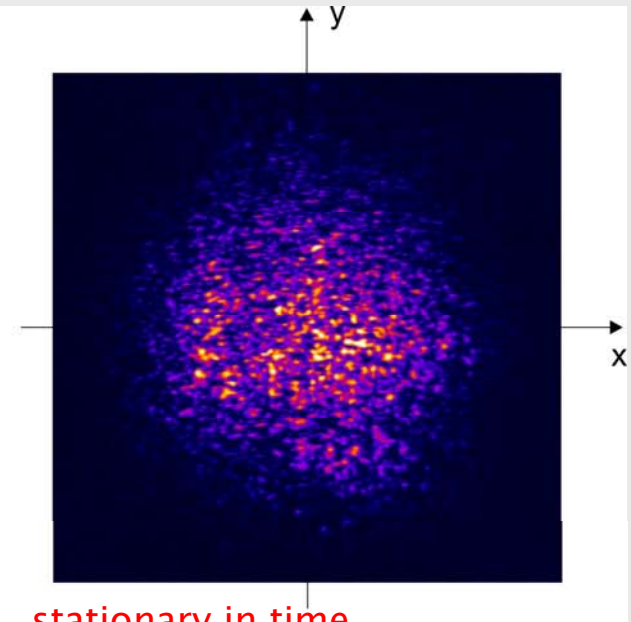
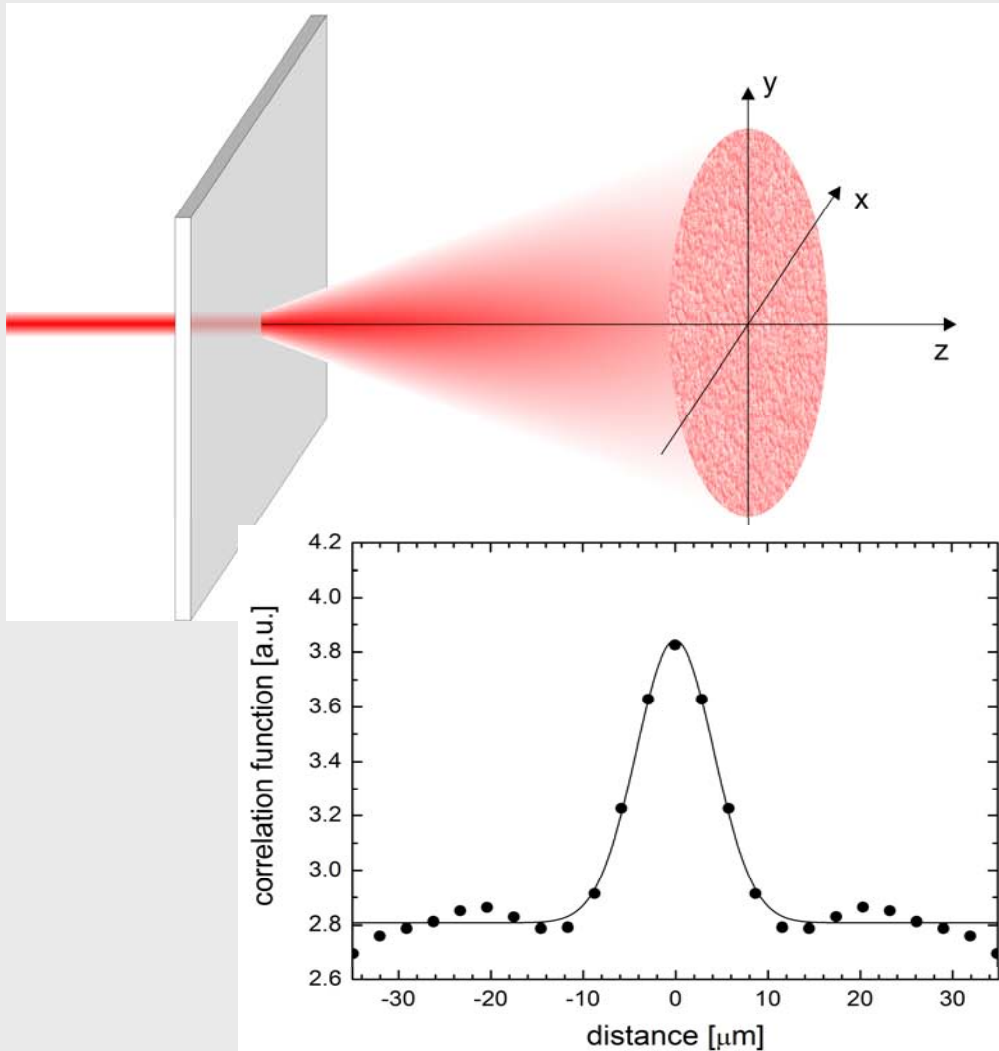


- ✓ quasiperiodic potential
- ✓ smaller length scale (1 μm or less)

Speckle optical potential

Lye et al., Phys. Rev. Lett. 95, 070401 (2005)
Fort et al., Phys. Rev. Lett. 95, 170410 (2005)

The random potential is produced by shining an off-resonant laser beam onto a diffusive plate and imaging the resulting speckle pattern on the BEC.



stationary in time
randomly varying in space

Width of speckle peaks diffraction
limited to $\sim 10 \mu\text{m}$

Bichromatic optical lattice: experimental scheme

main lattice

$\lambda_1 = 830 \text{ nm}$

$s_1 = 25$

$E_{R1} = 3.33 \text{ kHz}$

3D: x, y, z

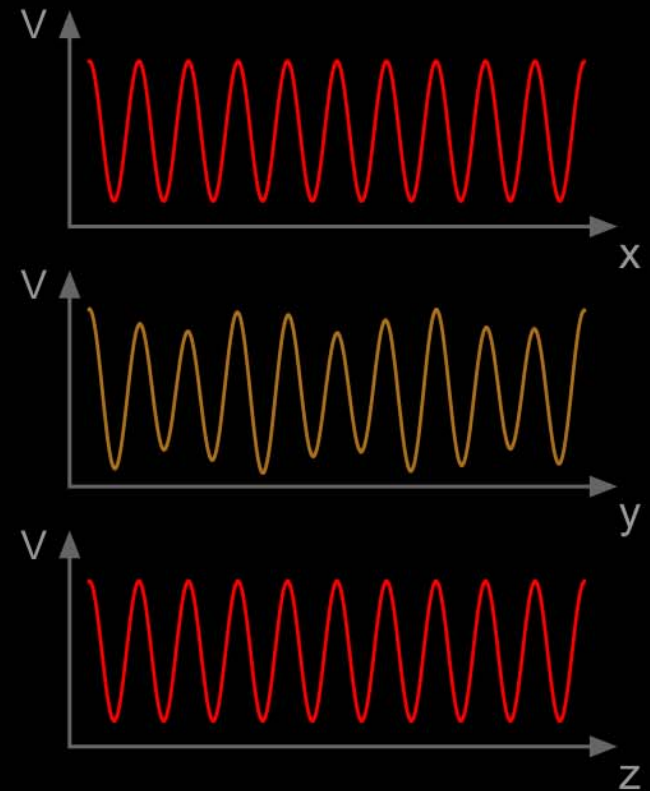
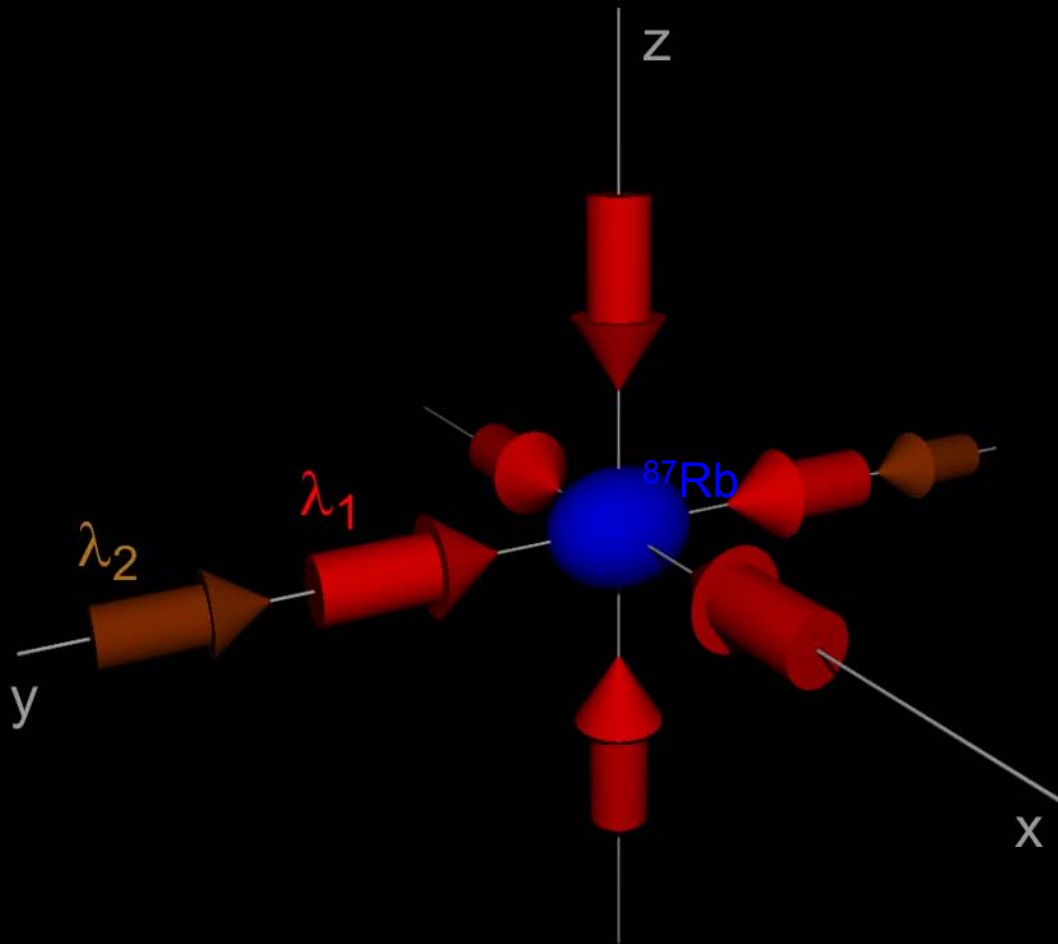
disordering lattice

$\lambda_2 = 1076 \text{ nm}$

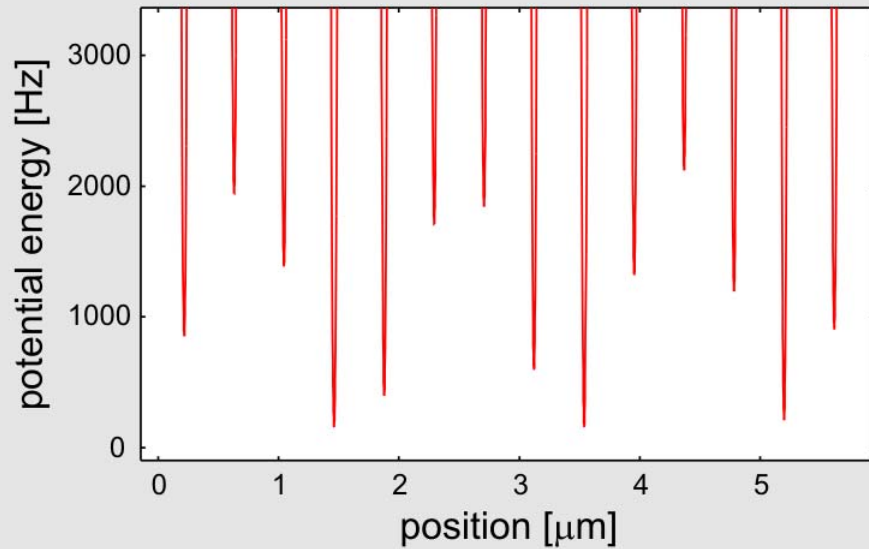
$s_2 = 0 \dots 3$

$E_{R2} = 1.98 \text{ kHz}$

1D: y



The “disordered” lattice

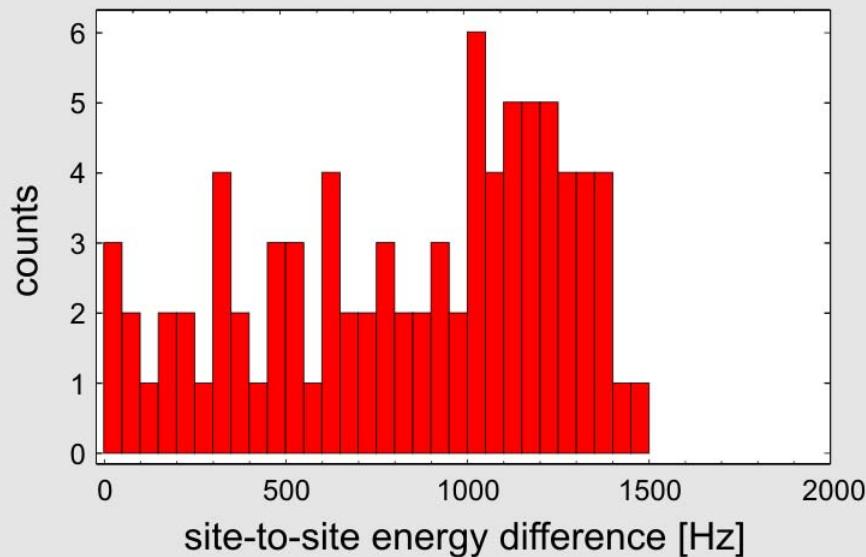


Energy minima of the lattice potential along y direction

Small variations induced by disordering lattice:

J constant within 5%

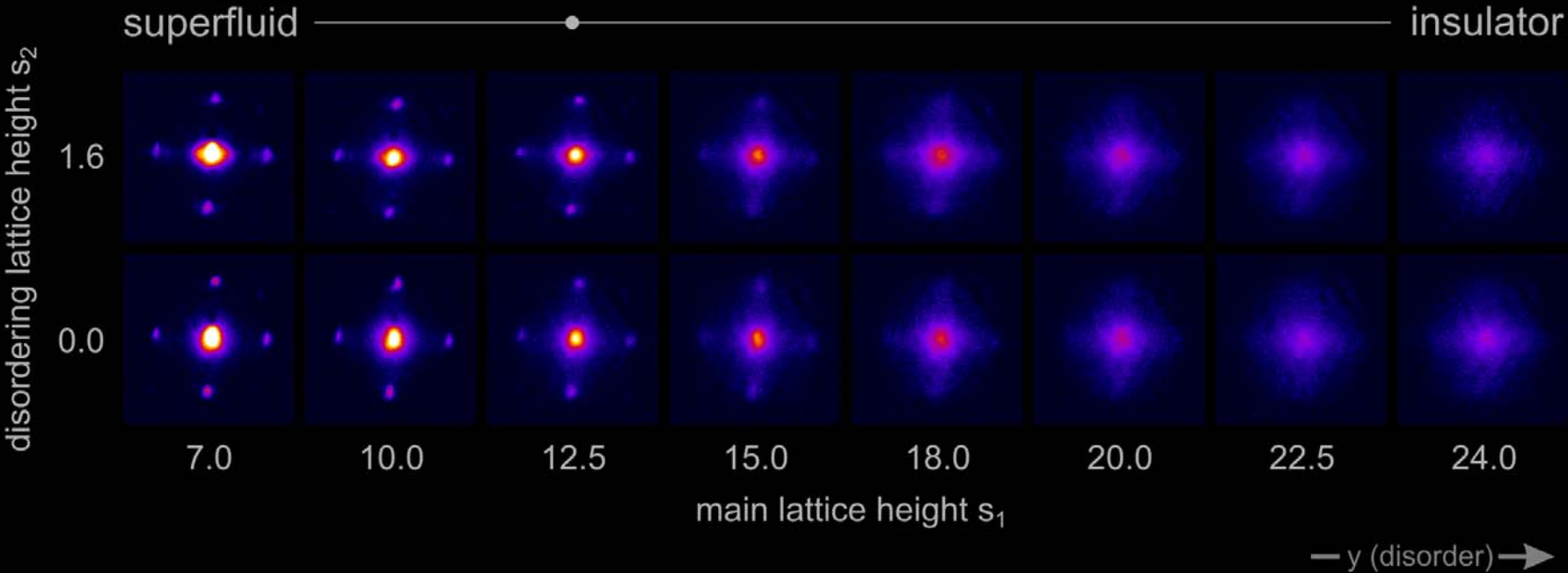
U constant within 1%



Distribution of the energy minima along y direction

Size of BEC 35 μm

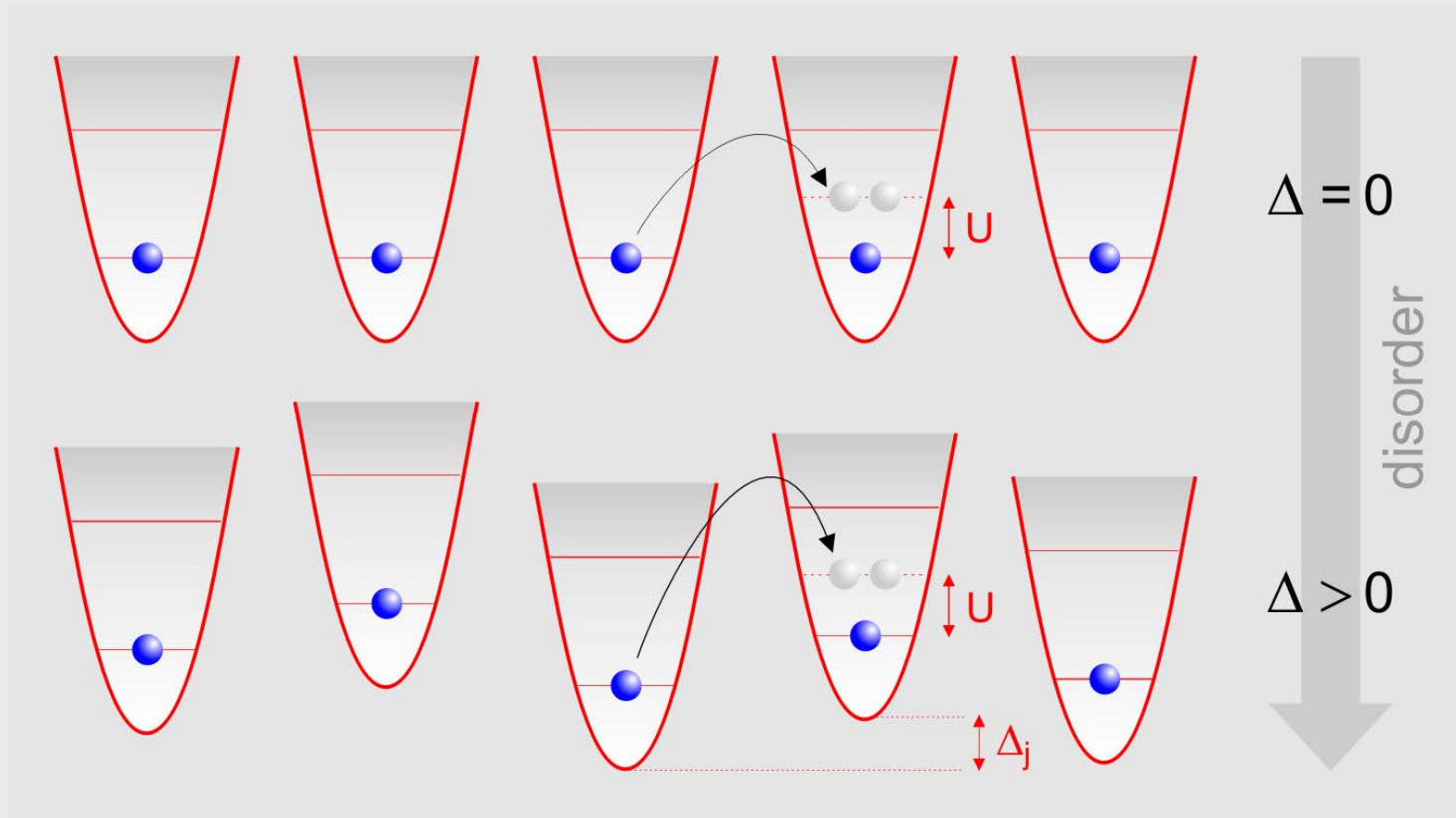
Entering the insulating states



No clear effect due to presence of disorder on interference patterns

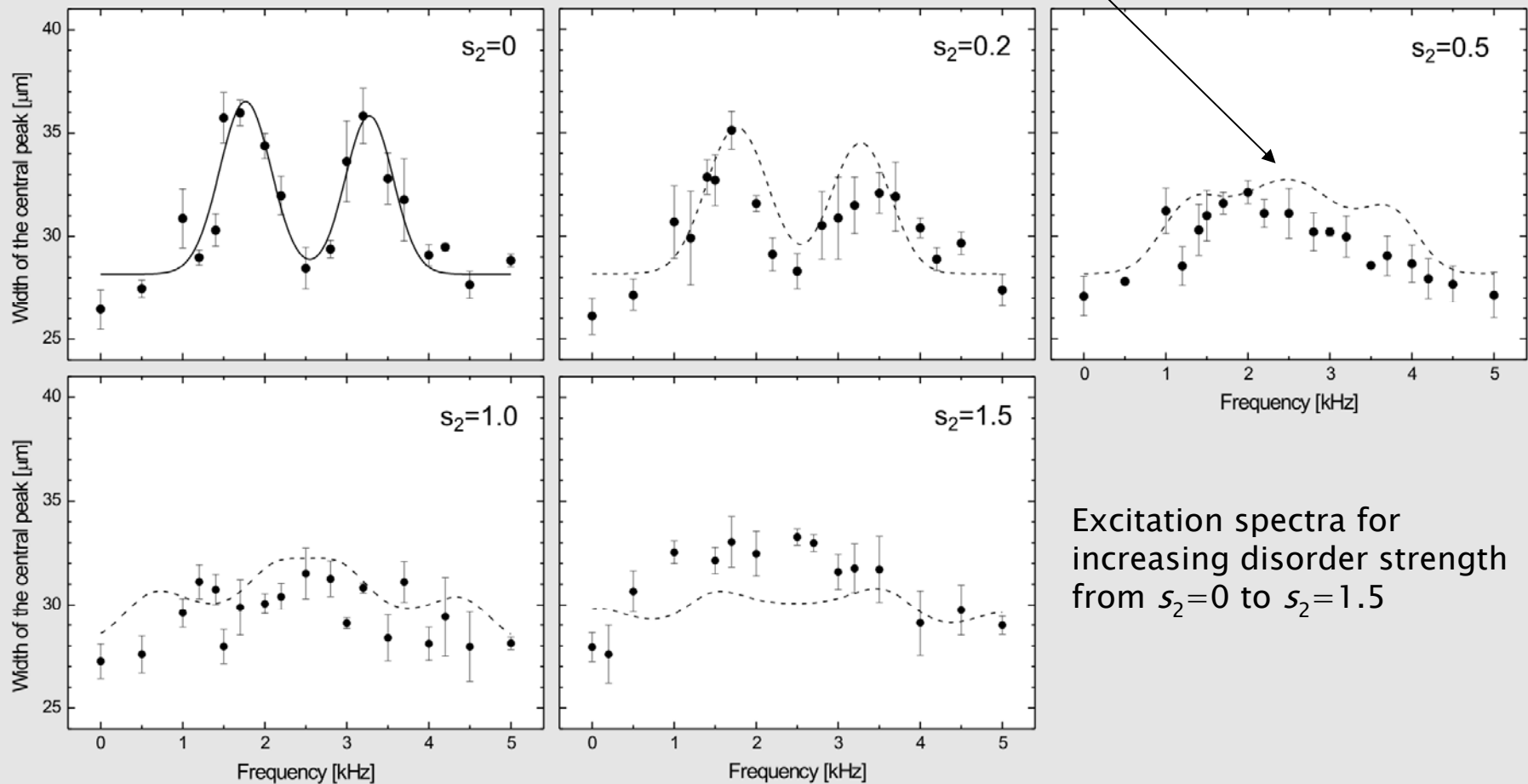
Broadening the Mott–Insulator spectrum

Starting from a Mott Insulator and adding disorder, the energy required for the hopping of a boson from a site to a neighboring one becomes a function of position

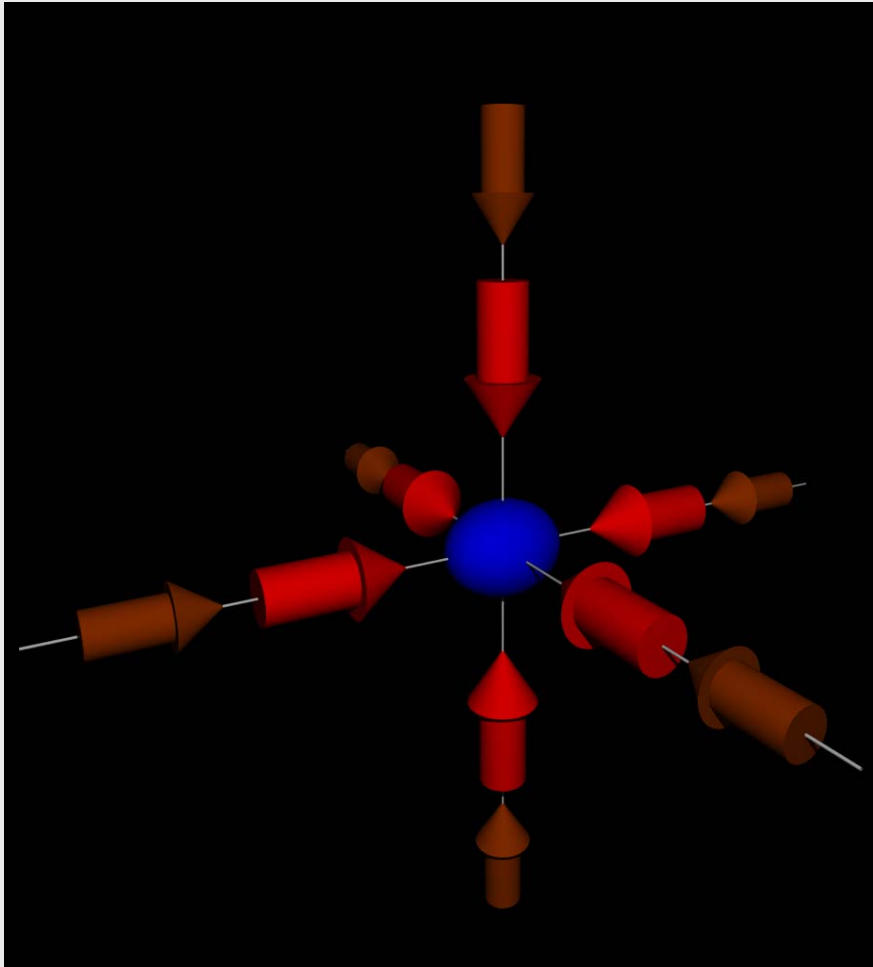


Excitation spectra

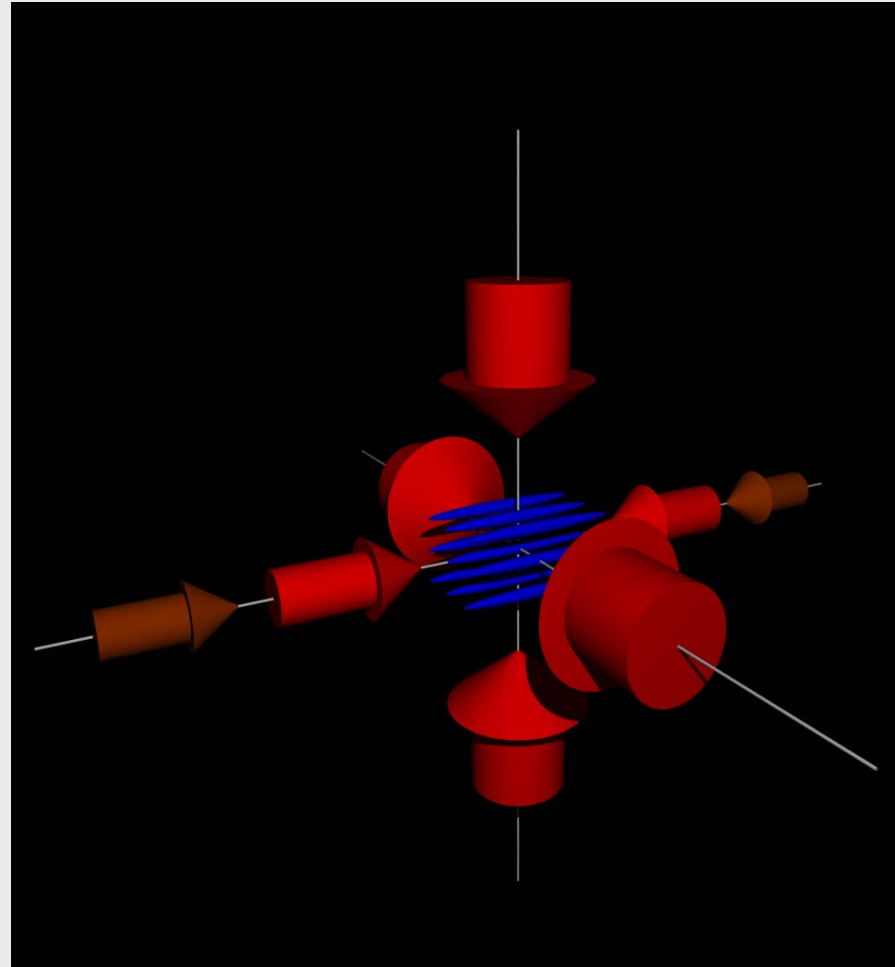
Convolution of the MI spectrum at $s_2=0$ with the distribution of site-to-site energy shifts



Further geometries



3D system + 3D disorder



1D systems ("tubes") + 1D disorder

Bose–Einstein condensates in periodic and disordered potentials

- Superfluid to Mott insulator transition
- Disordered potentials

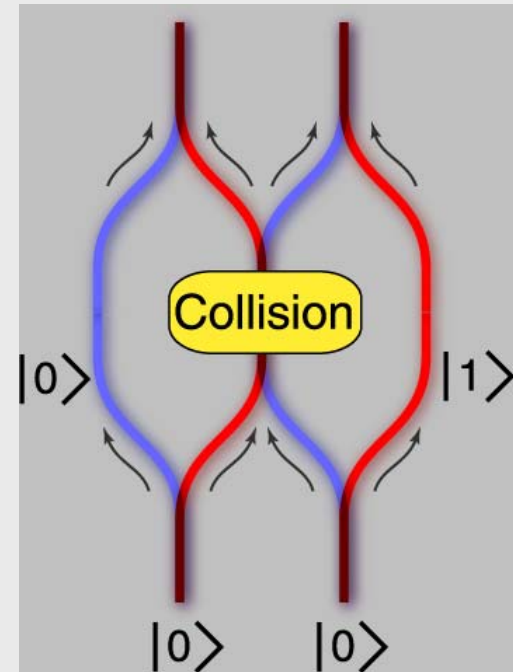
Quantum degenerate mixtures

- Ultracold heteronuclear molecules
- Attractive condensates for Quantum Measurements

Why ultracold heteronuclear molecules

Conditional dynamics with neutral atoms

- Only short range interactions, need to bring atoms in the same lattice site
- Weak interactions, slow gate, time $\tau \sim \text{ms}$
- To date only massive entanglement, no 2-qubits gate on specific sites



Ultracold collisions with Quantum degenerate mixtures

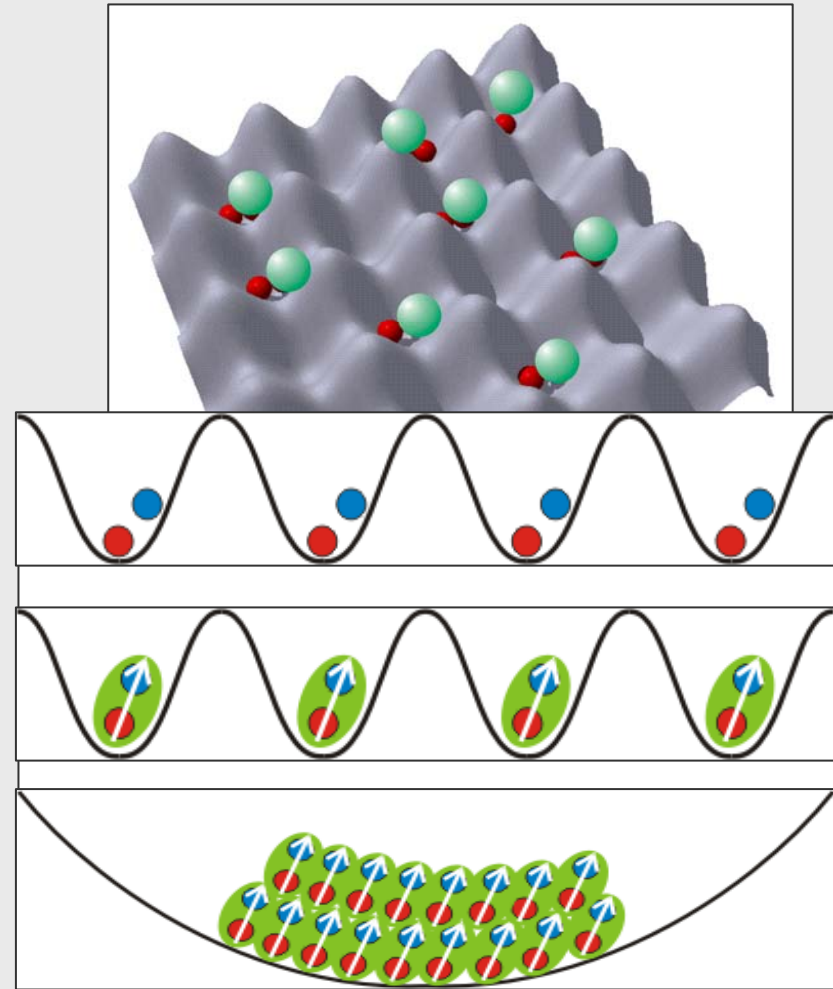
- Heteronuclear molecules can have electric dipole moments $d \sim 1 \text{ D}$
- Dipole-dipole interactions long-range ($1/R^3$)
- Several proposals to use molecules as addressable qubits

De Mille, Phys. Rev. Lett. 88 067901 (2002)

Feshbach-associated heteronuclear bosonic molecules

Double Mott-insulator phase:
one atom per specie in each lattice site
 $a_{12} \ll a_{11}, a_{22}$

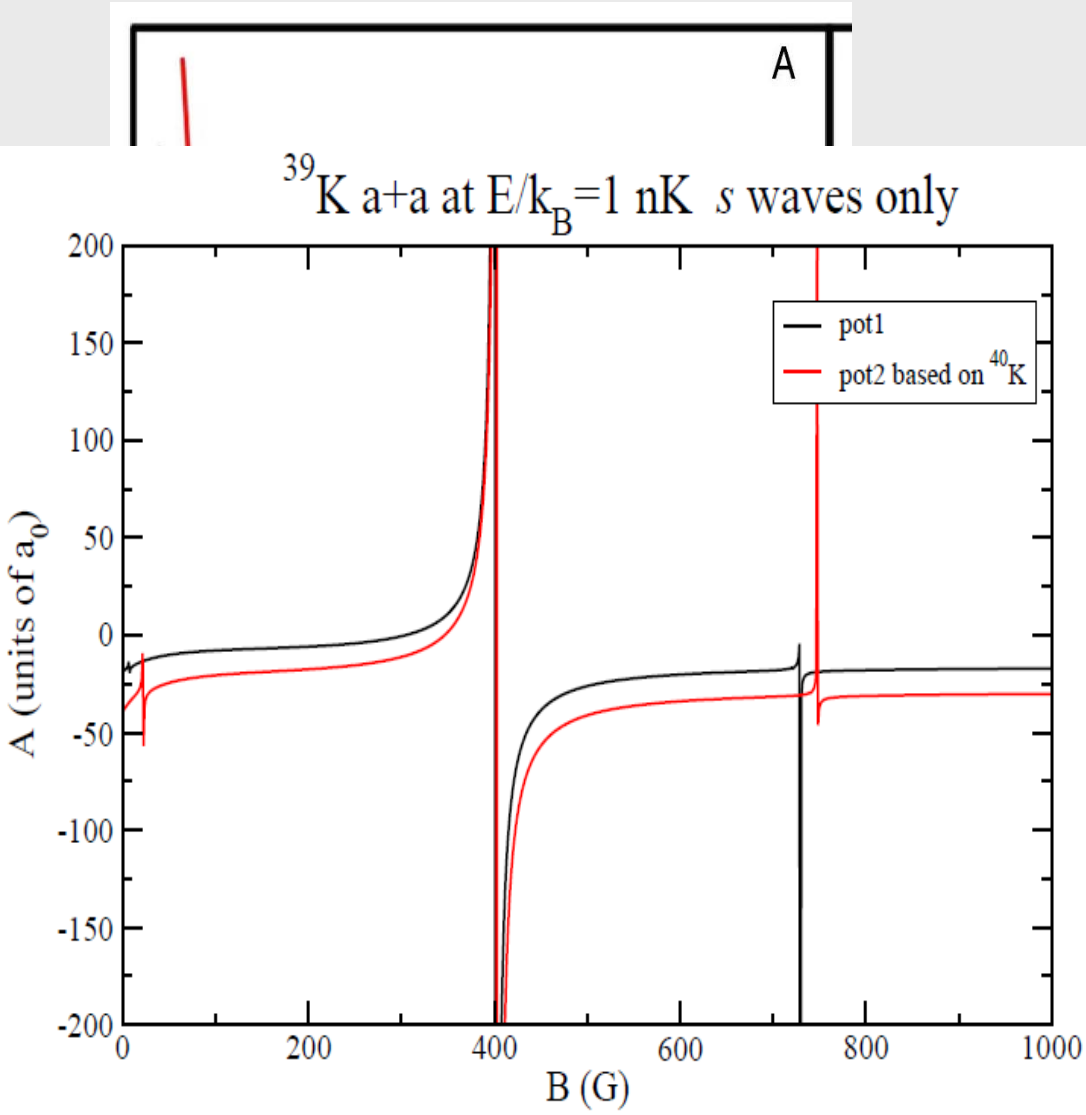
- Feshbach association of heteronuclear bosonic molecules
- no 3-body losses, shortening molecules lifetime
- Difficulty:
transfer to ground vibration state where $d \sim 0.25 D$



B. Damski et al., PRL. 90, 110401 (2003)
M. G. Moore et al., PRA 67, 041603 (2003)

Fano-Feshbach resonances

Scattering resonances due to input state energy nearly coincident with bound level in a different scattering channel. Energy coincidence driven by applied magnetic field.



Enhancement of the scattering length, displaying a dispersive behavior vs magnetic field

On the side of $a > 0$ the molecular state is lower in energy than the input state
→ Feshbach assisted molecular association

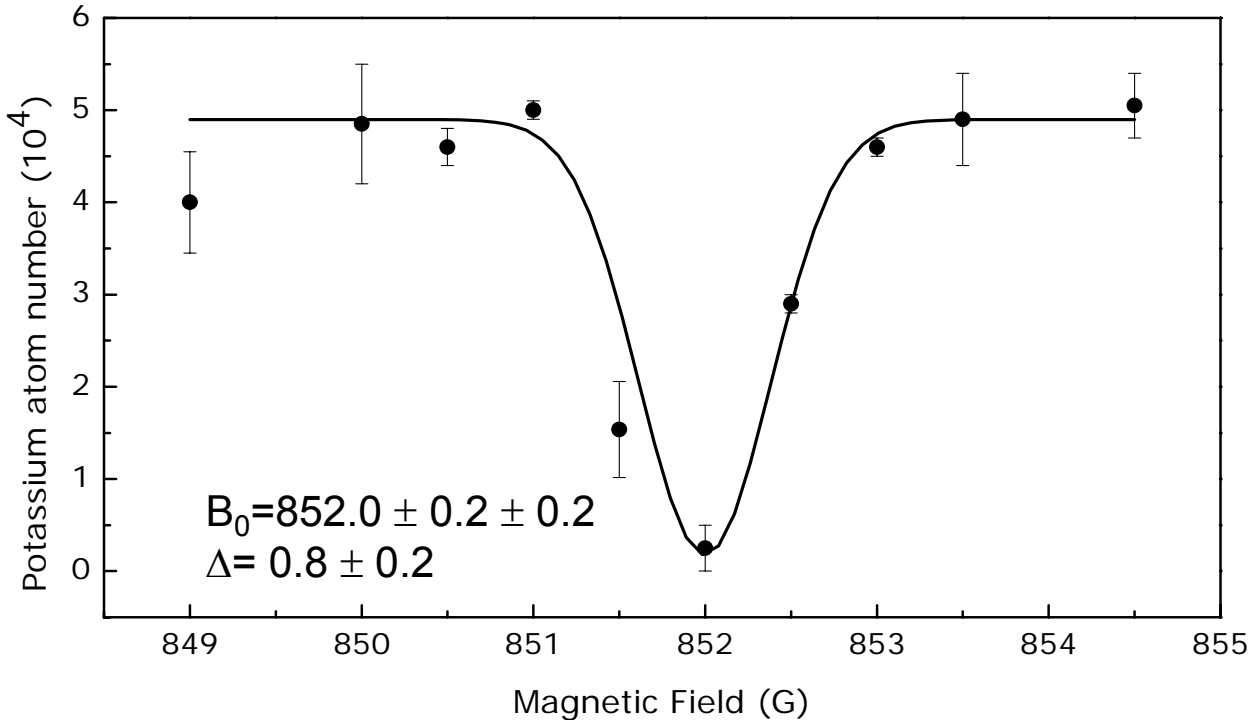
(unpublished, courtesy of A. Simoni)

Fano-Feshbach spectroscopy via atom losses

Rb

K

B (G)



854

LENS results and identification

- Some 14 resonances observed at LENS in the range 300 – 850 G
F. Ferlaino et al., Phys. Rev. A 73 040702(R) (2006)
Erratum, Phys Rev A 74 039903 (2006)
- Fit with numerical calculations (A. Simoni) → scattering lengths for 40K–87R
- Mass scaling to predict scattering lengths and FF resonances for other isotopes combinations

TABLE II: Calculated singlet and triplet *s*-wave scattering lengths for collisions between K and Rb isotopes. Sensitivity parameters $\beta_{s,t}$ to the number of bound states (Eq. 1 in Ref. [1]) are also shown, with power of ten displayed in parenthesis.

K-Rb	$\bar{a}_s (a_0)$	β_s	$\bar{a}_t (a_0)$	β_t
39-85	26.5 ± 0.9	-2.8(-2)	63.0 ± 0.5	-1.3(-2)
39-87	824^{+90}_{-70}	-1.5(-2)	35.9 ± 0.7	-1.6(-2)
40-85	64.5 ± 0.6	-3.9(-3)	-28.4 ± 1.6	-1.8(-2)
40-87	-111 ± 5		-215 ± 10	
41-85	106.0 ± 0.8	3.6(-3)	348 ± 10	6.5(-3)
41-87	14.0 ± 1.1	2.6(-2)	163.7 ± 1.6	7.7(-3)

TABLE III: Predicted zero-field *s*-wave scattering lengths for the absolute ground state of K-Rb isotopes. Feshbach resonance positions and widths are also provided for three selected isotopic pairs. The quoted uncertainties do not include the uncertainty on the number of bound states.

K-Rb	$a (a_0)$	$B_{th} (G)$	$\Delta_{th} (G)$
39-85	56.6 ± 0.4		
39-87	27.9 ± 0.9	248.8 ± 1.6	0.26
		320.1 ± 1.6	7.9
		531.9 ± 1.2	2.7
		616.2 ± 1.5	0.10
40-85	-21.3 ± 1.6		
40-87	-185 ± 7		
41-85	283 ± 6	132.5 ± 0.6	0.19
		141.2 ± 1.1	$2 \cdot 10^{-4}$
		147 ± 2	0.025
		184.6 ± 1.0	2.9
		191.4 ± 1.0	0.81
		660 ± 3	3.4
41-87	1667^{+790}_{-406}	687 ± 2	16
		17 ± 5	45
		67 ± 3	8.9
		516 ± 7	82
		688 ± 8	0.059

K-Rb mixture for attractive condensates

Explore new single species:

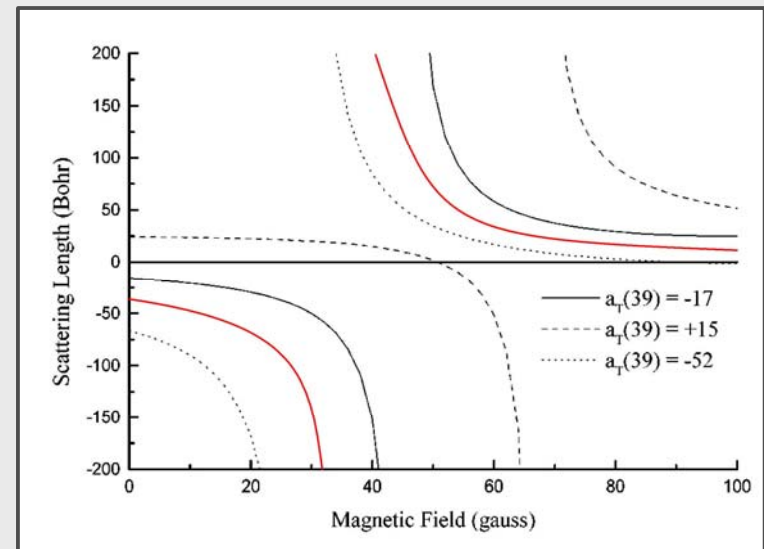
- Bose condensate of K39 for tunable interactions

attractive interactions: $a_t = -(33 \pm 5)a_0$, $a_s = -(45 \pm 15)a_0$

H.Wang et al., Phys. Rev. A 62, 052704 (2000)

wide Fano-Feshbach resonance predicted around 40 G

J. Bohn et al, Phys. Rev. A 58 3660 (1999)



J. Bohn et al, Phys. Rev. A 58 3660 (1999)

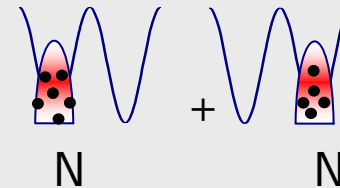
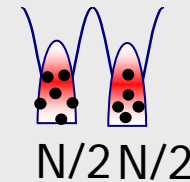
Maximally entangled states with attractive condensates

Bose-Hubbard hamiltonian

$$H = -J \sum_{\langle j,i \rangle} \hat{b}_j^\dagger \hat{b}_i + \sum_i \epsilon_i \hat{n}_i + \frac{1}{2} U \hat{n}_i (\hat{n}_i - 1)$$

- $J \gg U$ coherent state
- $|U| \gg J, U > 0$ Mott insulator
- $|U| \gg J, U < 0$ superposition of localized states, Schroedinger cats

$$|\psi\rangle = \frac{1}{\sqrt{MN!}} \sum_{j=1}^M e^{i\phi_j} \hat{b}_j^{\dagger N} |\text{vac}\rangle$$

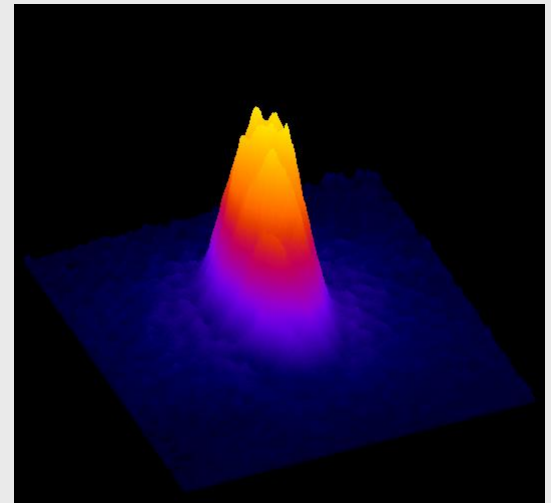
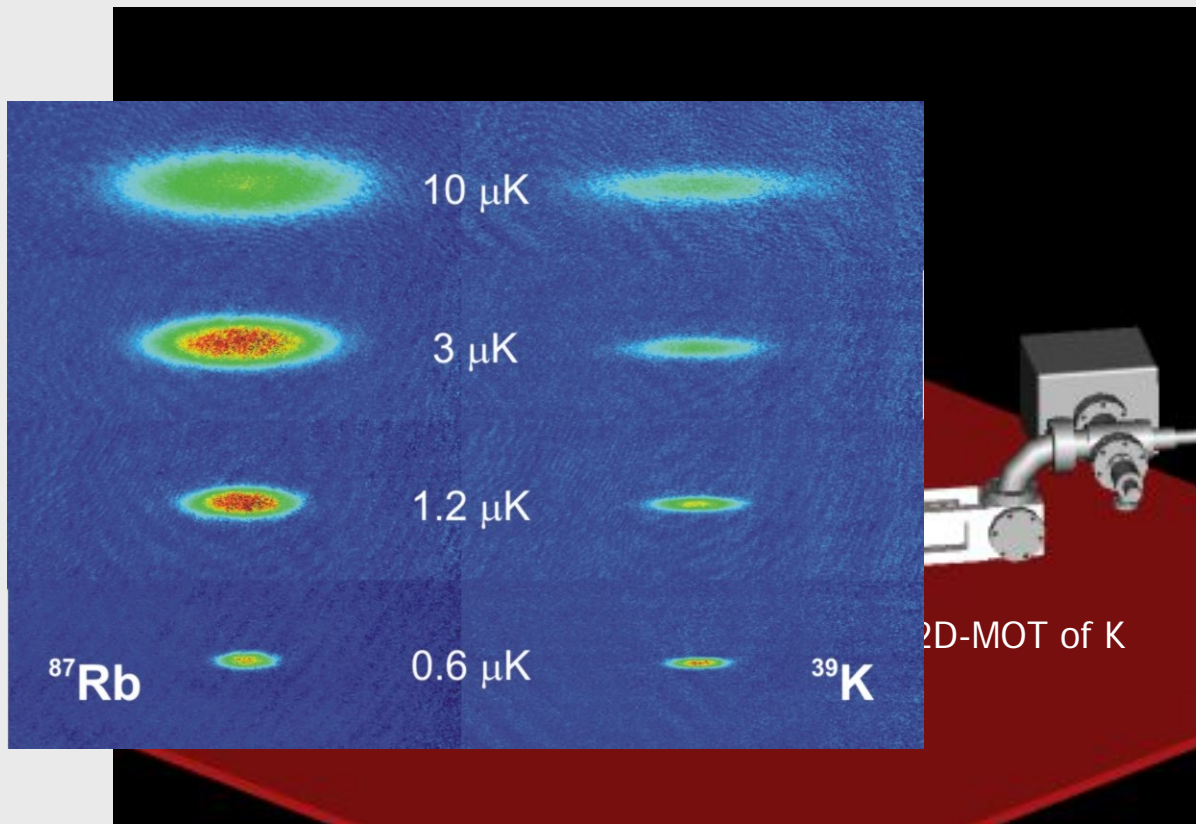


P. Buonsante et al., Phys. Rev. A 72, 043620 (2005)

Interferometry with S-cats overcomes Standard Quantum Limit $\Delta G/G \sim 1/\sqrt{N}$

Decoherence & detection open issues

Status of the experiment



- ☒ 2 dimensional MOT of Rubidium
- ☒ 2 dimensional MOT of Potassium
- ☒ Dual 3D-MOT
- ☒ Magnetic trapping and evaporation

- ☒ BEC of Rb
- ☒ Sympathetic cooling of K39, K41
- ☒ Double BEC of Rb-K
- ☒ Optical trap and lattice @ 1060 nm
- ☒ Fano-Feshbach resonances

Conclusions

- Onset of Bose-glass phase on 3D optical lattice disordered along 1D
- Fano-Feshbach resonances observed for Rb87-K40, precise determination of scattering lengths
- New Bose-Bose experiment: already single BEC, close to double BEC

Perspectives (Bose-Bose experiment)

- Fano-Feshbach resonances in K-Rb and in K-K
- Superfluid to Mott insulator phase transition with two species

Quantum Degenerate Gases team at LENS – Florence



Permanent members:
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Massimo Inguscio

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Modugno, G. Roati, *P. Maioli*

PhDs:
J. Catani, L. De Sarlo, V.
Guerrera, M. Zaccanti, C.
D'Errico

The end

Thanks

<http://quantumgases.lens.unifi.it>

(coming soon)